CS 229 Stanford

Ch1 Supervised Learning

1. **Gradient descent**: a search algorithm that starts with some “initial guess” of parameters, and that repeatedly changes parameters to make cost function smaller.
2. **Batch gradient descent** : In a single step, take entire training set to update parameters.

**Stochastic (Incremental) gradient descent** : BGD has to scan through the entire training set, which makes a costly operation when data size is large.

1. **To preform supervised Learning, we have to decide functions/hypothesis that map X to Y.**
2. **Linear Regression**
   1. 1st way : Set Cost function as MSE using Gradient Descent
   2. 2nd Way : Given MSE, we can apply Normal Equations to represent parameters mathematically.
   3. Why MSE for regression problem?
      1. Probabilistic Interpretation:
         1. Assumption: Y = Theata^T \* X + error , Error ~IID N(0,. Sigma^2)
         2. P(Y|X ; theta) = normal distribution and it can be regarded as likelihood function.
         3. Maximize log likelihood 🡨🡪 minimize MSE
   4. Locally Weighted Linear Regression (Non-parametric algorithm)
      1. If there is sufficient data, this makes the choice of features less critical.
      2. Weight is exp( - | x\_i - x | ) and x is the point to evaluate, so if difference is small, w is close to 1, and if the difference term is large, w will be small.
      3. Therefore, parameters are chosen giving a much higher “weight” to the errors on training examples close to the query point.
      4. Parametric vs. Non-Parametric
         1. While parametric learning algorithm has fixed, finite number of parameters, and after we’ve fit the parameters, training data is no more needed. Non-Pararmetric way means the amount of stuff we need to keep in order to represent the hypothesis h grows exponentially with the size of the training set.
3. **Classification and Logistic Regression**
   1. While linear regression takes h(x) as Theta\*X , Logistic regression takes h(x) as 1/(1+e^(-theta\*X)), non-linear function of Theta\*X , called logistic function or sigmoid function.
   2. Probabilistic way: Log-likelihood maximization
      1. P(y=1 | x; theta) = h(x), P(y=0 | x; theta) = 1 – h(x)
      2. P(y | x, theta) = h(x)^y \* (i-h(x))^(1-y ) using Bernoulli Distribution.
      3. By taking cost function as Likelihood function and set :



Same update rule with linear regression problem.

**Newton’s Method**

**Although it requires fewer iterations to get value close to minimum, it’s more expensive than gradient descent ( because it requires us to calculate n by n Hessian )**

**When Newton’s method is applied to maximize the logistic regression log-likelihood, resulting method is called Fisher Scoring**

When the goal is to find parameter theta 🡪 F(theta) = 0



What if the goal is to maximize function l? 🡪 points where its first derivative l’(theta) = 0. F(theta) = l’(theta)

🡪 C:\Users\09732\AppData\Local\Microsoft\Windows\INetCache\Content.Word\캡처2.png



**Generalized Linear Models**

Classification using logistic regression or perceptron algorithm 🡪? Find a decision boundary

**Discriminative** : Learn P(Y|X) directly or learn mapping directly from the space of input X to the labels

**Generative** : model P(X|Y) 🡪 model the distribution of a label’s feature.

After modeling p(y) – class priors, and p(x|y), we can apply Bayes rule to derive the posterior distribution on y given x.

1. **Gaussian Discriminant Analysis**
   1. **Assumption : P(X|Y) ~ multivariate normal distribution**
   2. **Compressed vs. Spread-out**
   3. **P(X|Y) is multivariate Gaussian 🡪 P(Y|X) follows a logistic function. But, not the other way around. : GDA makes stronger Assumption.** 
      1. **When such modeling assumption(P(X|Y) is Gaussian) is correct, GDA performs better**
      2. **With weaker assumptions, logistic regression is more robust and less sensitive to incorrect modeling assumptions. (Possion data (Non-Guassian data )🡪 Logistic Ok, but not for GDA )**
2. **Naïve Bayes**
   1. **X : discrete**
   2. **Example : X: Text, Y: Spam or Not (Text Classification)**
      1. **Represent an email via a feature vector whose length is equal to the number of words in dictionary**
      2. **Build a generative model : P(X|Y) 🡪 2^50000 possible outcomes.**
      3. **Therefore, make an assumption that observations of X are conditionally independent given y. (Naïve Bayes Assumption), which results Naïve Bayes Classification 🡪 e.g. knowledge of word “buy” doesn’t affect your beliefs about the word “price” occurrence.**
   3. **When the original, continuous-valued attributes are not modeled by a multivariate normal distribution, discretizing the features and using Naïve Bayes will often result in a better classifier.**
   4. **Laplace Smoothing**